THE UNIVERSITY OF WESTERN AUSTRALIA

Computer Science and Software Engineering

SEMESTER 1, 2016 EXAMINATIONS

CITS1001
Object-oriented Programming and Software Engineering

FAMILY NAME: _____ GIVEN NAMES: _____

STUDENT ID: | | | | | | | | | SIGNATURE: _____

This Paper Contains: **20** pages **(including title page)**
Time allowed: **2:00 hours (including reading time)**

INSTRUCTIONS:
Answer all questions. The paper contains eight questions, each worth ten marks.
Write your answers in the spaces provided on this question paper.
No other paper will be accepted for the submission of answers.
Do not write in this space.

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Class structure

1a) Write a Java class `Country` to represent a country that is a member of the European Union. The class should have

- three instance variables that capture a country's name, the year it joined the EU, and whether it uses the Euro as its currency;
- a constructor that sets up each of these variables (no error-checking is required);
- accessor methods for each of these variables; and
- a mutator method for the Euro variable. **(4 marks)**

1b) Write a Java class `EU` to represent the member countries of the European Union. The class should have

- one instance variable that contains information about the member countries;
- an accessor method that takes an integer and that returns the corresponding `Country` object;
- a method `newMember` that takes a `Country` object and updates the instance variable appropriately; and
- a method `needFX` that takes two `Country` objects and returns true iff you need to change currency when moving from one to the other. **(6 marks)**

Use this space and the following page for your answer to this question

```
public class Country
{
    private String name; private int year; private boolean euro;

    public Country(String name, int year, boolean euro)
    {
        this.name = name;
        this.year = year;
        this.euro = euro;
    }

    public String getName()
    {return name;}

    public int getYear()
    {return year;}

    public boolean usesEuro()
    {return euro;}

    public void joinEuro(boolean b)
    {euro = b;}
}
```

```
import java.util.ArrayList;

public class EU
{
    private ArrayList<Country> members;

    public Country getCountry(int k)
    {return members.get(k);}

    public void newMember(Country c)
    {members.add(c);}

    public boolean needFX(Country c1, Country c2)
    {
        return !c1.usesEuro() || !c2.usesEuro();
    }
}
```

Numbers

2) Write the three methods marked `TODO` below.

```
public class Rectangle
{
    // bottom-left and top-right corners of a rectangle
    // with sides are parallel to the axes
    private double blX, blY, trX, trY;

    public Rectangle(double x1, double y1, double x2, double y2)
                throws Exception
    {
        if (trX <= blX || trY <= blY)
           throw new Exception("invalid coordinates");
        blX = x1;
        blY = y1;
        trX = x2;
        trY = y2;
    }

    // returns the area of the rectangle
    public double area()
    {
        // TODO                                                    (2 marks)
    }

    // returns true iff the point x,y is inside the rectangle
    public boolean inside(double x, double y)
    {
        // TODO                                                    (3 marks)
    }

    // moves the top-right corner to form the largest square
    // that fits inside the original rectangle
    public void largestSquare()
    {
        // TODO                                                    (5 marks)
    }
}
```

Use this space and the following page for your answer to this question

```
// returns the area of the rectangle
public double area()
{
    return (trX - blX) * (trY - blY);
}


// returns true iff the point x,y is inside the rectangle
public boolean inside(double x, double y)
{
    return blX < x && x < trX && blY < y && y < trY;
}


// moves the top-right corner to form the largest square
// that fits inside the original rectangle
public void largestSquare()
{
    if (trX - blX > trY - blY)
         trX = blX + trY - blY;
    else trY = blY + trX - blX;
}
```

Booleans

3a) Using only conditionals and relational operators, write the method `smallestPositive` that takes two numbers and returns the smallest positive one.
If neither argument is positive, it returns `0`.
For example, `smallestPositive(7,4)` and `smallestPositive(4,7)` both return `4`, `smallestPositive(7,-4)` and `smallestPositive(-4,7)` both return `7`, and `smallestPositive(-7,-4)` returns `0`. **(6 marks)**

```
// returns the smallest positive of x and y;
// or 0 for two non-positive arguments
public int smallestPositive (int x, int y)
```

3b) Using only logical (Boolean) operators, write the method `mixture` that takes three Booleans and returns `true` if and only if they contain at least one `true`, and also at least one `false`.
For example, `mixture(true,false,false)` and `mixture(false,true,true)` both return `true`, but `mixture(true,true,true)` returns `false`. **(4 marks)**

```
// returns true iff x,y,z are a mixture of true and false
public boolean mixture(boolean x, boolean y, boolean z)
```

Use this space and the following page for your answer to this question

```
// returns the smallest positive of x and y;
// or 0 for two non-positive arguments
public int smallestPositive(int x, int y)
    {
        if (x > 0)
           if (y > 0) if (x < y) return x; else return y;
           else       return x;
        else
        if (y > 0) return y;
        else       return 0;
    }


// returns true iff x,y,z are a mixture of true and false
public boolean mixture(boolean x, boolean y, boolean z)
    {
        return (x || y || z) && (!x || !y || !z);
    }
```

Arrays

4a) Write the method `middle` that takes an array `a` and returns a new array holding the middle third of `a`. You may assume that the length of `a` is a multiple of 3.
For example, `middle({5,4,1,6,3,2})` returns `{1,6}`. **(4 marks)**

```
// returns the middle third of a
public static int[] middle(int[] a)
```

4b) Write the method `reversed` that returns `true` if and only if the arrays `a` and `b` contain exactly the same elements, but in reversed order.
For example, `reversed({3,1}, {1,3})` returns `true`, but `reversed({3,1}, {2,3})` and `reversed({3,1}, {1,1,3})` both return `false`. **(6 marks)**

```
// returns true iff a and b contain the same elements, reversed
public static boolean reversed(int[] a, int[] b)
```

Use this space and the following page for your answer to this question

```
// returns the middle third of a
public static int[] middle(int[] a)
    {
        int n = a.length / 3;
        int[] z = new int[n];
        for (int i = 0; i < n; i++)
            z[i] = a[i + n];
        return z;
    }



// returns true iff a and b contain the same elements, reversed
public static boolean reversed(int[] xs, int[] ys)
    {
        if (xs.length != ys.length) return false;
        for (int i = 0; i < xs.length; i++)
            if (xs[i] != ys[ys.length - 1 - i])
               return false;
        return true;
    }
```

Display

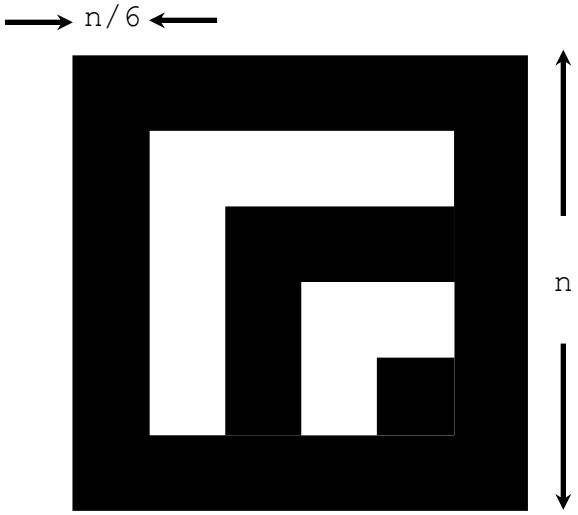
5) For the following questions, you may assume that both `java.awt.Color` and `SimpleCanvas` have been imported.

a) Write the method `flip` that takes a colour as its argument. If the argument is white, it returns black; if the argument is black, it returns white; if the argument is anything else, it throws an `IllegalArgumentException`. **(3 marks)**

```
// returns the opposite colour to col
public Color flip(Color col)
```

b) Use `flip` and the `SimpleCanvas` method `drawSq` below to write the method `drawNoland` that draws the flag of Noland, as illustrated below. The flag must be square with side `n`, and the width of each stripe must be one-sixth of `n`. **(7 marks)**

```
// draws a square of side s and colour c on its canvas,
// with its top-left corner at x,y
public void drawSq(int x, int y, int s, Color c)
```




```
// draws the flag of Noland with side n
public void drawNoland(int n)
```

Use this space and the following page for your answer to this question

```
// returns the opposite colour to col
public Color flip(Color col)
    {
        if (col == Color.black) return Color.white;
        else
        if (col == Color.white) return Color.black;
        else
        throw new IllegalArgumentException("Bad colour");
    }
```

```
// draws the flag of Noland with side n
public void drawNoland(int n)
    {
        int d = n / 6;
        SimpleCanvas sc = new SimpleCanvas();
        Color col = Color.black;
        sc.drawSq(0, 0, n, col);
        for (int i = d; i < n; i = i + d)
        {
            col = flip(col);
            sc.drawSq(i, i, n - i - d, col);
        }
    }
```

Data compression

6) One obvious way to compress binary data is to count the 0s and 1s, and to represent sequences of one digit as a single number. Thus a String sequence like "00100111" would be compressed to "2,1,2,3". The first number in the compressed sequence is always the number of initial 0s, so a sequence like "1101111" would be compressed to "0,2,1,4".

a) Write the method `compress` that takes a String `s` containing only 0s and 1s, and returns a compressed version of `s`. **(5 marks)**

```
// returns a compressed version of s
public static String compress(String s)
```

b) Write the method `uncompress` that takes a String `s` containing only digits, and returns an uncompressed version of `s`. **(5 marks)**

```
// returns an uncompressed version of s
public static String uncompress(String s)
```

Use this space and the following page for your answer to this question

```
public static String compress(String s)
    {
        String z = "";
        int c = 0;
        int count = 0;
        for (int k = 0; k < s.length(); k++)
            if (s.charAt(k) == '0' + c)
                count++;
            else
            {
                z = z + count + ",";
                c = 1 - c;
                count = 1;
            }
        return z + count;
    }
```

```
public static String uncompress(String s)
    {
        String z = "";
        for (int n = 0; n < s.length(); n++)
            for (int k = 0; k < s.charAt(n) - '0'; k++)
                z = z + n % 2;
        return z;
    }
```

Sorting

7) One of the fastest known sorting algorithms is *Heapsort*. The key phase of this algorithm reorders an array `a` of integers so that two properties hold for all indices `k`:

`a[k] >= a[2k+1]` and `a[k] >= a[2k+2]`

This phase of Heapsort is implemented by the method `heapify`.

```
// heapify(a) turns a into a heap in-place
public void heapify(int[] a)
{
  for (int root = a.length / 2 - 1; root >= 0; root--)
  {
    boolean done = false;
    while (2 * root + 1 < a.length && !done)
    {
      int swap = root;
      if (a[swap] < a[2 * root + 1])
         swap = 2 * root + 1;
      if (2 * root + 2 < a.length && a[swap] < a[2 * root + 2])
         swap = 2 * root + 2;
      if (swap == root)
         done = true;
      else
      {
         int temp = a[root];
         a[root] = a[swap];
         a[swap] = temp;
         root = swap;
      }
    }
  }
}
```

a) Show how the application `heapify({1,2,3,4,5,6,7,8,9})` is processed. In particular, show the state of `a` every time it is changed by `heapify`. **(7 marks)**

b) For what data will `heapify` be especially fast? **(3 marks)**

Use this space and the following page for your answer to this question

1	2	3	4	5	6	7	8	9	
1	2	3	9	5	6	7	8	4	swap 4,9
1	2	7	9	5	6	3	8	4	swap 3,7
1	9	7	2	5	6	3	8	4	swap 2,9
1	9	7	8	5	6	3	2	4	swap 2,8
9	1	7	8	5	6	3	2	4	swap 1,9
9	8	7	1	5	6	3	2	4	swap 1,8
9	8	7	4	5	6	3	2	1	swap 1,4

It will be fastest for data which is already sorted.

Recursion

8a) What is the role of the *base cases* in a recursive Java method? **(2 marks)**

8b) Exponentiation can be implemented efficiently using the following equations.

$x^0 = 1$
$x^{2n} = (x^2)^n$
$x^{2n+1} = x^{2n} * x$

Write the recursive method `exp` that calculates x^n using this algorithm. **(5 marks)**

```
// returns x raised to the power n
public static double exp(double x, int n)
```

8c) Show the sequence of method calls that your definition generates for the invocation `exp(3,6)`. **(3 marks)**

Use this space and the following page for your answer to this question

They tell the method when to stop; they return a result directly.

```
// returns x raised to the power n
public static double exp(double x, int n)
    {
        if (n == 0)     return 1;
        else
        if (n % 2 == 0) return exp(x * x, n / 2);
        else            return exp(x, n - 1) * x;
    }
```

```
   exp(3, 6)
→  exp(9, 3)
→  exp(9, 2) * 9
→  exp(81,1) * 9
→  exp(81,0) * 81 * 9
→  1 * 81 * 9
→  729
```

END OF PAPER