

# CITS5501 Software Testing and Quality Assurance Specifications in Alloy

Unit coordinator: Arran Stewart

May 15, 2018

## Sources

- Pressman, R., *Software Engineering: A Practitioner's Approach*, McGraw-Hill, 2005
- Huth and Ryan, *Logic in Computer Science*
- Pierce et al, *Software Foundations vol 1*
- Alloy tutorial at <http://alloytools.org>
- Jackson, *Software Abstractions*, 2006, MIT Press.

## Using Alloy

- We've seen how you can express signatures in Alloy, which represent entities of some sort.
- We'll now explore some of the other constructs Alloy permits, and how they can be used to explore and check a model.

## Language constructs

- *signatures*. We have seen these – they permit entities, and their relationships to other entities, to be declared.
- *functions*. Functions define a way of getting a set or relation given particular parameters.
- *predicates*. Predicates define formulas which evaluate to true or false, and can take parameters which are used in determining the result.
- *facts*. We have seen these – they act as *constraints*. They are deemed to be always true.
- *modules*. Similar to programming languages, we can organize Alloy specifications into modules.
- *assertions*. These also evaluate to true or false; but rather than being facts we declare to be true, they are things we would like Alloy to *check*.

## “Running” models

- We can *check* assertions – we ask Alloy to create instance of our model (up to a certain size), and look for counterexamples to our assertions.
- We can also find instances that satisfy *predicates*.

## Example

- Consider the following specification:

```
sig Name, Addr {}  
sig Book {  
  addr: Name -> lone Addr  
}
```

- If we'd like Alloy to generate some instances of this, we do so by asking it to generate instances that satisfy a *predicate*.

## Example – predicates

Here are some sample predicates:

- A predicate that takes no arguments, and is true if  $2 < 3$ :

```
pred myPred() {  
  2 < 3  
}
```

- A predicate that takes one argument,  $a$ , and is true if  $a < 3$ :

```
pred myPred(a : Int) {  
  a < 3  
}
```

## Example – predicates

- If we have *no* formula inside a predicate, the body is assumed to just be “true”:

```
pred myPred() {  
}
```

## Running predicates

- Let's ask Alloy to generate some instances. Initially, we won't put any constraints on the instances, so we'll just use an empty (always true) predicate:

```
pred show () {}
```

- We run it like so:

```
run show for 3
```

The “3” is a *scope* size – how large a state space Alloy should explore. In this case, at most 3 objects of each signature will be created.

## Running predicates

- For our book example, let's limit the scope to just one Book, like this:

```
run show for 3 but 1 Book
```

We'll create at most 3 objects, *except* for Book, which we'll only create 1 of.

## Running predicates

- Often, we'll want to examine particular sorts of instance of our model.
- Alloy found us a basic instance that had a link from a single name to an address;  
let's try and find instance with more than one name.

```
pred show (b : Book) {  
    #b.addr > 1  
}
```

- This says we want more than one link, effectively. (# is the “cardinality” operator; it gives us the size of a set.)
- The Alloy GUI provides a range of options for visualizing the results.

# Consistency

- Can we have one name linking to more than one address?

```
pred show (b: Book) {  
  #b.addr > 1  
  some n: Name | #n.(b.addr) > 1  
}
```

- We'll explore the second line a bit.

# Function application

- Function application is where you apply a function to arguments: e.g.

```
Math.abs( -3.0 );
```

- Alloy doesn't exactly have function *application*.
- Rather, it uses *joins*, which are more like the way a database operates.

## Function application

- Functions are a special sort of relation, in which something on the “left” uniquely maps to something on the “right”.
- Imagine we have a relation between pets and owners (where pets can only have one owner):

(Fido, Alice)

(Coco, Bob)

(Rex, Alice)

- This is a function, because no pet appears twice in the relation.

## Function application

- If we also have a set of pets:

```
pets = { Fido, Coco, Rex, Blackie }
```

then we can construct the *join* of the set “pets”, and our relation (call it “pet\_owner”):

```
pets.pet_owner = {  
  (Fido,  Alice)  
  (Coco,  Bob)  
  (Rex,   Alice)  
}
```

- Some pets apparently don't have an owner, so this is a partial function; those pets don't end up in the joined relation.

## Function application

- If we had multiple functions, we can join them one after another.
- Suppose we have a mapping from pets to owners, and from owners to mothers:

`pets.pet_owner.mother`

- If  $s$  is a set and  $r$  is a function, then  $s.r$  is the result of joining  $r$  to  $s$ ; it's the *image* of the set  $s$  going forward through  $r$

# Consistency

- So, can we have one name linking to more than one address?

```
pred show (b: Book) {  
  #b.addr > 1  
  some n: Name | #n.(b.addr) > 1  
}
```

- The second line asserts that there exist some (one or more) names, such that (in normal notation) the size of `b.addr(n)` is greater than 1.
- Alloy tells us that nothing satisfies this predicate (unsurprisingly, because of how we defined our signatures).

# Consistency

- It's useful to periodically check to make sure that we haven't *over-constrained* our model ...  
(i.e., made it impossible for consistent instances to ever exist)
- ... and also to check that we have *enough* constraints.  
(i.e., the sorts of instances generated match up with our intentions.)

## Consistency

- So let's check that we can have the result of “function application” result in a set larger than one – i.e., there is more than one address mapped to.

```
pred show (b: Book) {  
  #b.addr > 1  
  #Name.(b.addr) > 1  
}
```

```
run show for 3 but 1 Book
```

- (This says to take the function `b.addr` for our book, and apply it to the set `Name`.)

# Operations

- We can also write predicates that represent *operations* on things;  
typically, they'll refer to the “before” and “after” states of those things.

```
pred add (b, b': Book, n: Name, a: Addr) {  
    b'.addr = b.addr + n -> a  
}
```

- Our predicate `add` is a constraint, and says that `b'.addr` is the union of `b.addr` and the tuple `(n,a)`.

# Operations

- If we want to see if we can find instances that satisfy this predicate, we'll want to enlarge the scope:

```
pred showAdd (b, b': Book, n: Name, a: Addr) {  
  add[b, b', n, a]  
  #Name.(b'.addr) > 1  
}
```

run showAdd for 3 but 2 Book

- Using the Alloy visualizer, we can see what the “before” and “after” books look like.
- In the predicate above, the “add” predicate is *invoked*. This is a bit more like traditional function application: we supply arguments to the predicate between square brackets.
  - (Earlier versions of Alloy used parentheses.)

# Operations

- We can write similar code for other operations, like “delete”, and check that our expected constraints hold.

## Advantages of using Alloy to check models

- Alloy allows us to build models incrementally.
- We can start with a small, simple model, and add features.
- Furthermore, it's much easier to see what our model *is* when it's not commingled with code.
  - Once an application becomes large, we can imagine that when written in Java (say), there is a great deal of implementation code that obscures the abstract model.

## Comparison with other methods – “model checking”

- We refer to this as “checking our model”; but note that “model checking”, on its own, refers to a different sort of formal method.
- “Model checking” on its own normally refers to using various sorts of temporal logic to explore the evolution of finite state machines, and see whether particular constraints hold.

## Comparison with other methods – proofs and verification

- Note that Alloy only generates model instances up to a certain size;
  - it doesn't *prove* that a model is consistent.
- However, often, if there is an inconsistency, it will show up in quite small models.

## Exercise

- How could we model the *natural numbers* in Alloy?
- How could we model the process of transferring money between two bank accounts?